

**TWO-SCALE THERMO-MECHANICAL ANALYSIS OF
MULTIDIRECTIONAL CARBON/CARBON COMPOSITES USING
IMAGE-BASED FINITE ELEMENT METHOD**

A Thesis submitted

In fulfilment of the requirements for the degree of

Doctor of Philosophy

By

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October 2020

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This Ph.D. work is dedicated to my Mother, Father and Teachers

Declaration by the Research Scholar

I hereby declare that the entire work embodied in this thesis is the result of investigations carried out by me in the School of Engineering, Indian Institute of Technology Mandi, under the supervision of **Dr. Rajneesh Sharma** (School of Engineering) and **Dr. Syed Abbas** (School of Basic Sciences), and that it has not been submitted elsewhere for any degree or diploma. In keeping with the general practice, due acknowledgements have been made wherever the work described is based on findings of other investigators.

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Declaration by the Research Advisors

We hereby certify that the entire work in the thesis entitled “**Two-Scale Thermo-Mechanical Analysis of Multidirectional Carbon/Carbon Composites using Image-Based Finite Element Method**” has been carried out by **Md Zahid** under our supervision in the School of Engineering, Indian Institute of Technology Mandi, and that no part of it has been submitted elsewhere for any degree or diploma. We further certify that this thesis has been prepared in conformity with the rules and regulations of the institute and has attained a standard required to award a Ph. D degree.

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Acknowledgments

First of all, I would like to express my heartiest gratitude to my supervisors, Dr. Rajneesh Sharma (School of Engineering (SE)), and Dr. Syed Abbas (School of Basic Sciences (SBS)), IIT Mandi for their exemplary guidance, motivation, and kind support during the entire course of this programme. I also thank them a lot for giving me their valuable time and golden suggestions that helped me in the academic field and made me capable of handling the critical situations in my personal life.

I would also like to thank my doctoral committee members, Dr. Rajeev Kumar (SE), Dr. Rajesh Ghosh (SE), Dr. Vishal Singh Chauhan (SE), and Dr. Amit Jaiswal (SBS), for their support and constructive suggestions which helped me improve my work and research skills.

I am also thankful to Prof. Puneet Mahajan, IIT Delhi, for providing me with an image processing facility and his fruitful suggestions. I would also like to thank Dr. Rohini Devi (Asso. Director), Dr. R.K Jain (Tech. Director), and Dr. Atul R Bhagat (Scientist-D), ASL, DRDO Telangana for providing me the composite specimen and experimental facilities. I am also grateful to Dr. A. Ganju (Director) and Mr. Paramvir Singh (Scientist-C) SASE, DRDO, Manali, and India to provide the scanning facility.

I am also thankful to my lab mates and friends Abhilash Awasthi, Sonalal Prasad, Ravi Sandal, Ashish Rehal, Sneha Das, Misbah Bashir, Farha Anjum, Kamran, Wasil, Chandar, Md. Amir, Ahmad Raza, Md. Shakir, and Md Sultan Alam for their support and making my stay joyful in the campus. Encouragement from friends of my graduation days, Nadeem, Saif (jangli), Meraj, Kashif (Chotka), Fahad, Kaify, and Shashi has always been like a positive source of energy for me and I will always remain thankful to them. I would also like to express my special thanks to my childhood friend Nuzhat Nahid (Goldy) for her continuous motivation and encouragement.

I am very grateful to my beloved wife, Hena Parween and my Son Mohammad Omar, for their love, motivation, patience, and being always there for me when I needed them the most. I am also thankful to

my in-law family members, relatives, especially my uncle Late Md. Zafaruddin, my cousin brother Arif bhaijaan, and my uncle Md Liyakat Ali for their admirable support and motivation.

I would like to express my deepest gratitude to my mother, Aqueela Begum, my father Md. Farooque, my younger brother Md. Shahid, my sweet sisters Nuzhat (Daisy) and Nikhat (Sana), for their love, motivation and support. I am also thankful to Akif Bhai, who is not less than my elder brother, for his selfless support to my family in my absence, which directly helped me in the smooth completion of my dissertation work. I am also thankful to my ustad, Qari Jahangir, my former teachers Mr. Ravi Panday, Mr. Zeeshan, Dr. Shahid Mahmood (NIT Patna) and Dr. Sikandar Azam (IIT Dhanbad), who continuously motivated me during my academic journey.

Above all, I thank Almighty Allah Subhanahu Wa Ta'ala for blessing me with all the happiness, kind people in the form of a guide, teachers, friends, family, relatives, and great opportunities and success in my life.

Mohammad Zahid

October 2020

Abstract

Carbon/Carbon (C/C) composites consist of carbon fibers and carbonaceous matrix as the main constituents. In these composites, the carbon fibers are oriented in different directions to achieve tailored properties. Two of such architectures are three-dimension hybrid (3DH) and four dimensions inplane (4DIN) C/C composites widely used in thermal protection systems in aerospace applications. These composites are very popular in the applications where the dimensional stability of structures is highly needed under severe thermo-mechanical loading conditions. Therefore, in the present study, these composites have been studied in detail using the image-based finite element method and two-scale asymptotic homogenization scheme. This includes some of the inherent geometrical imperfections directly in the finite element meshes and also accounts for the micro-structure hierarchy.

First of all, the 2D images of these composites were reconstructed using an X-ray computed tomography facility. The inherent imperfections that are primely raised during the heat treatment procedure of fabrication were explored. The inherent imperfections were categorized as voids (Micro voids and big voids), cracks (intra-bundle, matrix, and interfacial), and bundle distortions. With the help of 2D images of microstructure, a three-dimensional (3D) model of these composites was reconstructed and discretized into finite element mesh. The resulting finite element model of realistic microstructure successfully included some of the inherent imperfections such as irregularly shaped big voids and bundle distortion directly.

Further, two-scale asymptotic expansion homogenization was utilized under periodic boundary conditions to predict the effective thermo-mechanical properties such as effective thermal conductivity and effective thermal expansion coefficient. The Laser flash experiment was performed to measure the effective thermal conductivity of 3DH C/C composite in the in-plane direction up to 1000°C for the numerical model's validity. The measured TC is found in a very good agreement with predicted results that successfully validate the proposed IBFE model. The effect of interfacial debond was also incorporated in terms of effective thermal gap conductance that caused a decrease in the effective thermal conductivity of the composite. In the case of 3DH C/C composite, around 14.85% and 7.98 % reduction in the in-plane TC of the 3DH C/C composite was observed at 27°C and 1227°C respectively. However, the out-of-plane TC was reduced by 6.2 % and 2.8 % at the respective temperatures. On the other hand, TC was reduced by around 5% due to the imperfect interface for the full range of temperatures; thus, Interfacial debond shows a significant effect on the behavior of 3DH

C/C composite compared to 4DIN C/C composite. Further, it was observed that the local distribution of field variables (temperature and heat flux) is significantly affected due to the presence of imperfections. Next, the effective thermal expansion coefficients (CTEs) of these composites were studied. In the numerical predictions of effective CTEs of 4DIN C/C composite, the effect of the three interfacial conditions, namely i) perfectly bonded, ii) imperfectly bonded, and iii) completely debonded interface was included using surface-based cohesive behavior. The effective CTEs in x and z directions decreased significantly due to the imperfect interface, while opposite behavior was noticed for CTE in the y-direction. For the validation of numerical findings, effective CTEs of 4DIN C/C composite were measured experimentally in the temperature range of 200-2500 °C. The in-plane CTE varied from 0.56 to $2.66 \times 10^{-6}/^{\circ}\text{C}$. The predicted CTEs corresponding to the imperfect interface were found in very close proximity with experimental results. It was also found that interfacial damage initiates at around 247 °C with the corresponding strains of 0.008%, 0.06 %, and 0.009% in x, y, and z directions respectively. Finally, the thermal shock resistance (TSR) of 4DIN C/C composite was predicted in terms of critical laser power density as a function of laser beam diameter using the finite element-based simulation of laser pulse irradiation technique. The temperature dependency and anisotropic behavior of material were included in the analysis. A homogenous cylindrical body was assumed as a test specimen, and shear strength as a failure criterion. The yz-plane was predicted as a critical plane. The locations near the laser beam periphery around 1.5-2 mm below the irradiated surface were observed as the critical location for shear failure. Apart from this, the temperature and shear stress distribution at critical LPD values were studied in detail. It was noticed that the TSR of 4DIN C/C composite is 10-18 times higher than that of 2D C/C composite.

The presented study concludes that the IBFE method is an effective route to include the inherent imperfections realistically into the FE analysis. The microstructural imperfections such as voids, bundle distortion, and imperfectly bonded interfaces cause a significant reduction in effective thermo-mechanical properties of multidirectional C/C composites.

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